

GRADUATION PROFICIENCIES

GRADUATION PROFICIENCY \#1:
MATHEMATICAL REASONING AND COMMUNICATION

Students will reason mathematically to solve problems and communicate with others.

Proficiency \#1: Mathematical Reasoning and Communication
Proficiency \#2: Modeling
Proficiency \#3: Number and Quantity
Proficiency \#4: Functions and Algebraic Reasoning

Proficiency \#5: Geometry and Measurement

Proficiency \#6: Data, Statistics and Probability

PERFORMANCE INDICATORS:
Students will...

|  | K-2 | $\mathbf{c} \mathbf{3 - 5}$ | $\mathbf{6 - 8}$ | $\mathbf{9 - 1 2}$ |
| :--- | :--- | :--- | :--- | :--- |
| A | Observe, identify and <br> analyze situations in <br> order to ask questions <br> and understand and <br> describe problems. <br> (MP1, 2) | Observe, identify and <br> analyze situations in <br> order to ask questions <br> and understand and <br> describe problems. <br> (MP1,2) | Observe, identify and <br> analyze situations in <br> order to ask questions <br> and understand and <br> describe problems. <br> (MP1, 2) | Observe, identify and <br> analyze situations in order <br> to ask questions and <br> understand and describe <br> problems. (MP1, 2) |
| B | Select strategies and <br> appropriate tools to <br> develop and <br> implement a plan to <br> solve problems. <br> (MP1, 5) | Select strategies and <br> appropriate tools to <br> develop and <br> implement a plan to <br> solve problems. (MP1, <br> 5) | Select strategies and <br> appropriate tools to <br> develop and <br> implement a plan to <br> solve problems. (MP1, <br> 5) | Select strategies and <br> appropriate tools to <br> develop and implement <br> a plan to solve problems. <br> (MP1, 5) |
| C | Explain whether an <br> answer is <br> mathematically and <br> contextually <br> reasonable. (MP1, 6) | Explain whether an <br> answer is <br> mathematically and <br> contextually <br> reasonable. (MP1, 6) | Explain whether an <br> answer is <br> mathematically and <br> contextually <br> reasonable. (MP1, 6) | Explain whether an <br> answer is <br> mathematically and <br> contextually <br> reasonable. (MP1, 6) |
| $\mathbf{D}$ | Evaluate, justify, and <br> defend the relative <br> effectiveness of <br> problem solving <br> processes using <br> logical argument. <br> (MP1, 3) | Evaluate, justify, and <br> defend the relative <br> effectiveness of <br> problem solving <br> processes using <br> logical argument. (MP <br> 1, 3) | Evaluate, justify, and <br> defend the relative <br> effectiveness of <br> problem solving <br> processes using logical <br> argument. <br> (MP 1, 3) | Evaluate, justify, and <br> defend the relative <br> effectiveness of problem <br> solving processes using <br> logical argument. (MP1, 3) |

GRADUATION PROFICIENCIES

## GRADUATION PROFICIENCY \#1:

## MATHEMATICAL REASONING AND COMMUNICATION <br> (CONTINUED)

|  | K-2 | 3-5 | 6-8 | 9-12 |
| :---: | :---: | :---: | :---: | :---: |
| E | Precisely communicate mathematical understandings and connections using a variety of representations. (MP1, 3, 6) | Precisely communicate mathematical understandings and connections using a variety of representations. (MP1, 3, 6) | Precisely communicate mathematical understandings and connections using a variety of representations. (MP1, 3, 6) | Precisely communicate mathematical understandings and connections using a variety of representations. (MP1, 3, 6) |

GRADUATION PROFICIENCIES AND PERFORMANCE INDICATORS

Proficiency \#1: Mathematical Reasoning and Communication
Proficiency \#2: Modeling
Proficiency \#3: Number and Quantity

Proficiency \#4: Functions and Algebraic Reasoning
Proficiency \#5: Geometry and Measurement
Proficiency \#6: Data, Statistics and Probability

PERFORMANCE INDICATORS: Students will...

|  | K-2 | $\mathbf{c} \mathbf{3 - 5}$ | $\mathbf{6 - 8}$ | $\mathbf{9 - 1 2}$ |
| :--- | :--- | :--- | :--- | :--- |
| A | Create an appropriate <br> model using numbers, <br> quantities, and other <br> representations to <br> describe a relationship <br> in a real world <br> situation. (MP4) | Create an appropriate <br> model using numbers, <br> quantities, and other <br> representations to <br> describe a relationship <br> in a real world situation. <br> (MP4) | Create an appropriate <br> model using numbers, <br> quantities, and other <br> representations to <br> describe a relationship <br> in a real world situation. <br> (MP4) | Create an appropriate <br> model using numbers, <br> quantities, and other <br> representations to <br> describe a relationship in a <br> real world situation. (MP4) |
| B | Compare and critique <br> different models for <br> a real world situation. <br> (MP4) | Compare and critique <br> different models for <br> a real world situation. <br> (MP4) | Compare and critique <br> different models for <br> a real world situation. <br> (MP4) | Compare and critique <br> different models for a real <br> world situation. (MP4) |
| C | Apply models to real <br> world situations. (MP4) | Apply models to real <br> world situations. (MP4) | Apply models to real <br> world situations. (MP4) | Apply models to real <br> world situations. (MP4) |
| D | Interpret the results of <br> a mathematical model <br> in the context of the <br> original real world <br> situation. (MP4) | Interpret the results of <br> a mathematical model <br> in the context of the <br> original real world <br> situation. (MP4) | Interpret the results of <br> a mathematical model <br> in the context of the <br> original real world <br> situation and adjust the <br> model as needed. (MP4) | Interpret the results of a <br> mathematical model in the <br> context of the original real <br> world situation and adjust <br> the model as needed. <br> (MP4) |

GRADUATION PROFICIENCIES AND PERFORMANCE INDICATORS

## GRADUATION PROFICIENCY \#3:

## NUMBER AND QUANTITY

Students will reason, describe, and analyze quantitatively using number and units to solve problems.

PERFORMANCE INDICATORS: Students will...

Proficiency \#1: Mathematical Reasoning and Communication
Proficiency \#2: Modeling

Proficiency \#3: Number and Quantity

Proficiency \#4: Functions and Algebraic Reasoning
Proficiency \#5: Geometry and Measurement
Proficiency \#6: Data, Statistics and Probability

|  | K-2 | 3-5 | 6-8 | 9-12 |
| :---: | :---: | :---: | :---: | :---: |
| A | Use counting to identify quantities. (K.CC.1, 2, 4, 5, 6; 1.NBT.1; 2.OA.3; 2.NBT.2) | Explain and make generalizations about the patterns in the place value system. <br> (4.NBT.1, 2; 5.NBT.1, 2, 3) | Compute fluently with multi-digit numbers and find common factors and multiples. (6.NS.2, 3, 4) | Reason quantitatively and use units to solve problems. (HS.N-Q.A) |
| B | Explain and make generalizations about the patterns in the place value system. (K.NBT.1; 1.NBT.2, 3; 2.NBT.1, 2, 3, 4) | Perform single- and multi-digit arithmetic with the four operations with whole numbers and decimals using understanding of place value and the properties of operations. $\begin{aligned} & \text { (3.OA.1, 2, 5, 7; 3.NBT.1, } \\ & \text { 2, 3; 4.NBT.4, 5, 6; } \\ & \text { 5.OA.1; 5.NBT.4, 5, 6, 7) } \end{aligned}$ | Make and explain statements of order and comparison of rational numbers. (6.NS.5, 6, 7) | Perform arithmetic operations and solve equations involving complex numbers. (HS.N-CN.A.1,2; HS.N-CN.C.7) |

GRADUATION PROFICIENCIES AND PERFORMANCE INDICATORS

## GRADUATION PROFICIENCY \#3:

## NUMBER AND QUANTITY

(CONTINUED)

|  | K-2 | $\mathbf{3 - 5}$ | $\mathbf{6 - 8}$ | $\mathbf{9 - 1 2}$ |
| :--- | :--- | :--- | :--- | :--- |
| $\mathbf{C}$ | Perform single- and <br> multi-digit addition <br> and subtraction <br> with whole numbers <br> using understanding <br> of place value and <br> the properties of <br> operations. <br> (K.OA.2, 5; 1.OA.5, 6, <br> 8; 1.NBT.4, 5, 6; 2.OA.2; <br> 2.NBT.5, 6, 7, 8, 9) | Solve problems <br> involving measurement <br> concepts using all four <br> operations. <br> (3.MD.1; 4.MD.1, 2; <br> 5.MD.1) | Solve real world and <br> mathematical problems <br> involving the four <br> operations with rational <br> numbers. (6.NS.1; 7.NS.1, <br> 2, 3; 7.EE.3) |  |
| $\mathbf{D}$ | Solve problems <br> with addition and <br> subtraction involving <br> measurement <br> concepts. <br> (K.MD.2; 1.MD.A.3; <br> 2.MD.5, 6, 7, 8) | Solve fraction problems <br> with all four operations <br> by applying <br> understanding of <br> fraction as number, the <br> concept of equivalency, <br> and previous <br> understanding of <br> operations on whole | Identify irrational <br> numbers and <br> approximate them with <br> rational numbers. <br> (8.NS.1, 2; 8.EE.2) <br> (3.Nb.1, 2, 3; 3.G.2; |  |

GRADUATION PROFICIENCIES

GRADUATION PROFICIENCY \#4:
FUNCTIONS \& ALGEBRAIC REASONING

Students will create, interpret, use, and analyze expressions, equations and inequalities including recognizing when a relationship is a function and evaluating that function.

Proficiency \#1: Mathematical Reasoning and Communication
Proficiency \#2: Modeling

Proficiency \#3: Number and Quantity
Proficiency \#4: Functions and Algebraic Reasoning

Proficiency \#5: Geometry and Measurement
Proficiency \#6: Data, Statistics and Probability

## PERFORMANCE INDICATORS:

Students will...

|  | K-2 | 3-5 | 6-8 | 9-12 |
| :---: | :---: | :---: | :---: | :---: |
| A | Represent and solve problems (of all problem types) using the relationship between addition and subtraction. (K.OA.1, 2, 3, 4; 1.OA.1, 2, 4, 8; 2.OA.1) | Represent and solve problems (of all problem types) involving all four operations using the relationship between addition/subtraction and multiplication/division. (3.OA.3, 4, 6, 8; 4.OA.1, 2, 3) | Use properties to create and evaluate equivalent expressions. (6.EE.1, 2, 3, 4; 7.EE.1, 2; 8.EE.1, 2, 4) | Interpret the structure of expressions and use it to solve problems. (HS.ASSE.A, B; HS.A-APR.A, D.6) |
| B | Apply the concept of equality and properties of operations to solve problems. (1.OA.3, 7, 8) | Apply the concept of equality and the properties of operations to solve problems.* $(3.0 A .4,5)$ | Create and solve equations and inequalities in mathematical and real world problems. (6.EE.5-9; 7.EE.4) | Solve equations, systems, and inequalities symbolically and graphically. (HS.A-REI.B, C, D) |
| C | Observe and identify patterns and relationships. (K.CC.1, <br> 2, 3; K.NBT.1; 1.NBT.1, 2, 3; 2.OA.3; 2.NBT.1, 2, 3, 4) | Generate, analyze, and explain numerical patterns and relationships. (3.OA.9; 4.OA.4, 5; 5.OA.3; 5.NBT.2) | Analyze proportional relationships and use them to solve real world and mathematical problems. (6.RP.1, 2, 3; 7.RP.1, 2, 3; 7.G.1; 8.EE.5) | Use multiple representations to analyze and interpret functions in terms of their context. (HS.F-IF.B, C7) |

GRADUATION PROFICIENCIES AND PERFORMANCE INDICATORS

GRADUATION PROFICIENCY \#4:

## FUNCTIONS \& ALGEBRAIC REASONING

(CONTINUED)

|  | K-2 | 3-5 | $\mathbf{6 - 8}$ | $\mathbf{9 - 1 2}$ |
| :--- | :--- | :--- | :--- | :--- |
| D |  |  | Analyze, graph and solve <br> linear equations and <br> pairs of simultaneous <br> linear equations to solve <br> problems. (6.EE.9; <br> 8.EE.7, 8) | Build functions to model <br> relationships between <br> quantities. (HS.F-BF.A; HS.F- <br> LE.A, B) |
| E |  |  | Identify and compare <br> functions.(8.F.1, 2, 3) |  |
| F |  |  | Use functions to model <br> relationships between <br> two quantities. (8.F.4, 5) |  |
| G |  |  |  |  |

GRADUATION PROFICIENCIES AND PERFORMANCE INDICATORS

GRADUATION PROFICIENCY \#5:
GEOMETRY AND MEASUREMENT

Students will apply concepts of geometry, spatial reasoning, and measurement in the context of real world problems.

Proficiency \#1: Mathematical Reasoning and Communication
Proficiency \#2: Modeling
Proficiency \#3: Number and Quantity
Proficiency \#4: Functions and Algebraic Reasoning
Proficiency \#5: Geometry and Measurement
Proficiency \#6: Data, Statistics and Probability

PERFORMANCE INDICATORS:
Students will...

|  | K-2 | 3-5 | 6-8 | 9-12 |
| :---: | :---: | :---: | :---: | :---: |
| A | Describe and compare measurable attributes of objects. (K.MD.1, 2; 1.MD.1) | Graph points on the coordinate plane to solve real world and mathematical problems. (5.G.1, 2) | Use transformations to demonstrate congruence and similarity. (8.G.1, 2, 3, 4) | Use transformations to define congruence and similarity. <br> (HS.G-CO.A,B; HS.GSRT.A) |
| B | Create, identify, and distinguish between shapes based on their defining attributes. (K.G.1, 2, 3, 4, 5, 6; 1.G.1, 2; 2.G.1) | Identify, distinguish, and classify 2D and 3D geometric figures based on their properties. <br> (3.G.1; 4.G.1, 2, 3; 5.G.3, <br> 4) | Apply the Pythagorean Theorem and its converse to solve real world and mathematical problems. (8.G.7, 8) | Demonstrate and explain proofs of geometric theorems. (HS.G-CO.C; HS.G-SRT.B.4; HS.G-GC.1) |
| C | Use appropriate tools to measure. <br> (1.MD.2; 2.MD.1, 2, 3, 4) | Apply understanding of geometric measurement (angles, perimeter, area and volume) to solve real world problems. (3.MD.5, 6, 7; 4.MD.3, 5, 6, 7: 5.MD.3, 4, 5) | Apply understanding of geometric measurement (angles, length, area, surface area and volume) to solve real world problems. (6.G.1, 2, 3, 4; 7.G.4, 5, 6; 8.G.9) | Use geometric properties and theorems to solve problems. <br> (HS.G-SRT.B.5; C; HS.GC.A.1, 2, 3; B.5; HS.GGPE.B.4,5,7) |

GRADUATION PROFICIENCY \#5:

## GEOMETRY AND <br> MEASUREMENT

(CONTINUED)

|  | K-2 | 3-5 |  | $\mathbf{9 - 8}$ |
| :--- | :--- | :--- | :--- | :--- |
| D |  |  |  | Apply coordinate <br> geometry to solve <br> problems. <br> (HS.G-GPE.A.1, 2; B.6) |
| E |  |  |  | Solve problems involving <br> two- and three- <br> dimensional objects. <br> (HS.G-GMD.A, B) |
| F |  |  |  | Apply trigonometric <br> ratios to solve problems <br> involving right triangles. <br> (HS.G-SRT.C) |

GRADUATION PROFICIENCIES AND PERFORMANCE INDICATORS

GRADUATION PROFICIENCY \#6:
DATA, STATISTICS, AND PROBABILITY
Students will apply principles of statistics and probability to analyze and interpret data, reach and justify conclusions and make inferences and predictions.

Proficiency \#1: Mathematical Reasoning and Communication
Proficiency \#2: Modeling
Proficiency \#3: Number and Quantity
Proficiency \#4: Functions and Algebraic Reasoning
Proficiency \#5: Geometry and Measurement
Proficiency \#6: Data, Statistics and Probability

PERFORMANCE INDICATORS:
Students will...

|  | K-2 | $\mathbf{c}$ | $\mathbf{3 - 5}$ | $\mathbf{6 - 8}$ |
| :--- | :--- | :--- | :--- | :--- |
| A | Classify, organize <br> and represent data. <br> (K.MD.3; 1.MD.4; <br> 2.MD.9, 10) | Classify, organize and <br> represent data. <br> (3.MD.3, 4; 4.MD.4; <br> 5.MD.2) | Organize and represent <br> bivariate data. (6.SP.4; <br> 8.SP.1, 2, 4) | Summarize, represent, and <br> interpret data. <br> (HS.S-ID.A, B, C) |
| B | Interpret and use <br> information from data <br> sets to solve problems. <br> (1.MD.4; 2.MD.10) | Interpret and use <br> information from data <br> sets to solve problems. <br> (3.MD.3; 4.MD.4; <br> 5.MD.2) | Summarize, describe <br> and make inferences <br> about distributions of <br> data. (6.SP.2, 3, 5; 7.SP.3, <br> 4; 8.SP.1, 3, 4) | Use data to make <br> inferences and justify <br> conclusions from sample <br> surveys, experiments, and <br> observational studies. <br> (HS.S-IC.A, B) |
| C |  |  | Use random sampling to to <br> draw inferences about a <br> population. (7.SP.1, 2) | Use the concept of <br> dependence and rules of <br> probability to compute <br> probabilities. (HS.S-CP.A; <br> B.6, 7) |
| D |  |  | Develop, use, and <br> evaluate probability <br> models. (7.SP.C) |  |

